

# The relevance of $\gamma_L^*$ in hard collisions of virtual photons

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- Virtual photon and its “structure”
- PDF of  $\gamma_L^*$  in QED
- QCD improved PDF of  $\gamma_L^*$
- Relevance of  $\gamma_L^*$  in hard collisions
- Future
- Conclusions

**Related work:****Contributions of  $\gamma_L^*$ :**

- J. Ch., M. T.:* Eur. Phys. J. C 16 (2000),  
hep-ph/0003300, phenomenology with  $\gamma_L^{\text{QED}}$
- J. Ch.:* Phys. Lett. B, QCD corrections to QED  
formulae for PDF of  $\gamma_L^*$
- J. Ch., M. T.:* in preparation, partly in this talk  
phenomenology with QCD improved PDF of  $\gamma_L^*$

**General aspects of virtual photon interactions:**

- J. Ch., J. Cvach:* in *Future Physics at HERA*
- J. Ch., M. T.:* in *MC Generators for HERA*,  
hep-ph/9905444
- J. Ch., M. T.:* in *PHOTON'99*, hep-ph/9906552
- J. Ch., M. T.:* hep-ph/9912514,
- M. Taševský:* PhD Thesis, H1 data vs NLO JETVIP  
calculations including the resolved  $\gamma_T^*$
- C. Friberg, T. Sjöstrand:* Eur. Phys. J. C13 (2000), 151  
also emphasizes the relevance of  $\gamma_L^*$

## Structure of the virtual photon

Data relevant to the concept of  $\gamma^*$  “structure”

**PLUTO:** 1984,  $F_{\text{eff}}^\gamma(x, P^2, Q^2)$  for  $\langle P^2 \rangle = 0.35 \text{ GeV}^2$

**H1** - dedicated analyses:

1. **Phys. Lett. B415 (1997), 418:**  $\sigma^{\text{res}}$  from single jets in the range  $0 \leq P^2 \leq 49 \text{ GeV}^2$
2. **Eur. Phys. J. C13 (2000), 397:**  $D_{\text{eff}}(x, P^2, Q^2)$  from dijets in the range  $1.6 \leq P^2 \leq 80 \text{ GeV}^2$
3. **M. Taševský's PhD Thesis: dijets vs JETVIP, NLO QCD** calculations including the resolved  $\gamma_T^*$  contributions,  $1.44 \leq P^2 \leq 25 \text{ GeV}^2$ . The most detailed NLO QCD analysis of data on  $\gamma^*$

**H1** - several other papers ( $R_2$ , forward jets) use the concept of virtual photon structure to improve the agreement of LO MC with data

**ZEUS:**  $r(Q^2) \equiv \sigma^{\text{res}}/\sigma^{\text{dir}}(P^2)$  for  $0 \leq P^2 \leq 4 \text{ GeV}^2$ , claims failure of JETVIP, **but  $r(Q^2)$  unsuitable** for comparison with parton level QCD!

**TPC/2 $\gamma$ :**  $\sigma_{\text{tot}}(\gamma\gamma^*(P^2))$ ,  $0.2 \leq P^2 \leq 60 \text{ GeV}^2$

**TOPAZ:**  $\sigma_{\text{tot}}(\gamma\gamma^*(P^2))$ ,  $1 \leq P^2 \leq 37 \text{ GeV}^2$

**L3:**  $F_{\text{eff}}^\gamma(x, P^2, Q^2)$  for  $0 \leq P^2 \leq 6 \text{ GeV}^2$ , exhibits very **puzzling  $P^2$  dependence!!**

## Basic concepts and formulae

Fluxes of photons from incoming electron

$$f_{\gamma_T/e}(y, P^2) = \frac{\alpha}{2\pi} \left( \frac{2(1-y) + y^2}{y} \frac{1}{P^2} - \frac{2m_e^2 y}{P^4} \right)$$

$$f_{\gamma_L/e}(y, P^2) = \frac{\alpha}{2\pi} \frac{2(1-y)}{y} \frac{1}{P^2}, \quad P_{\min}^2 = \frac{m_e^2 y^2}{1-y}$$

The difference at **large**  $y$  crucial for separation of  $\gamma^T, \gamma^L$

Cross sections of hard collisions of virtual photons

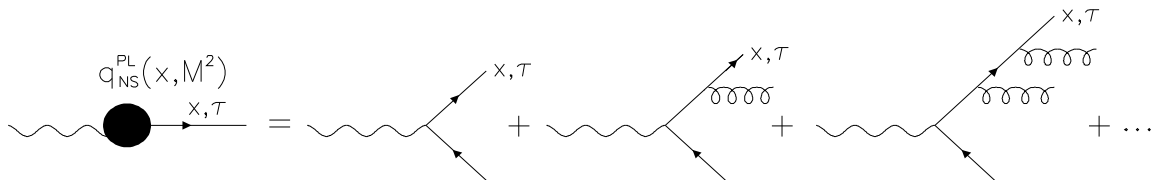
$$\sum_{k=T,L} f_{\gamma_k/e} \otimes \sum_{i=q,\bar{q},G} f_{i/\gamma_k} \otimes \sigma_i$$

PDF  $f_{i/\gamma^k}$  of the photon can be written as sums of **hadronic** (HAD) and **pointlike** (PL) parts

$$f(x, P^2, Q^2) = f^{\text{HAD}}(x, P^2, Q^2) + f^{\text{PL}}(x, P^2, Q^2)$$

This separation is, however, **ambiguous!**

**Pointlike part** of NS quark distribution function results from the resummation



describing QCD corrections to QED. In units of  $3e_q^2\alpha/2\pi$

$$q_k^{\text{QED}} = f_k(x) \ln \left( \frac{Q^2}{xP^2 + m_q^2/(1-x)} \right) - f_k(x) + \frac{g_k(x)m_q^2 + h_k(x)P^2}{xP^2 + m_q^2/(1-x)}$$

$$f_T(x) = x^2 + (1 - x)^2, \quad g_T(x) = \frac{1}{1 - x}, \quad h_T(x) = 0,$$

$$f_L(x) = 0, \quad g_L(x) = 0, \quad h_L(x) = 4x^2(1 - x)$$

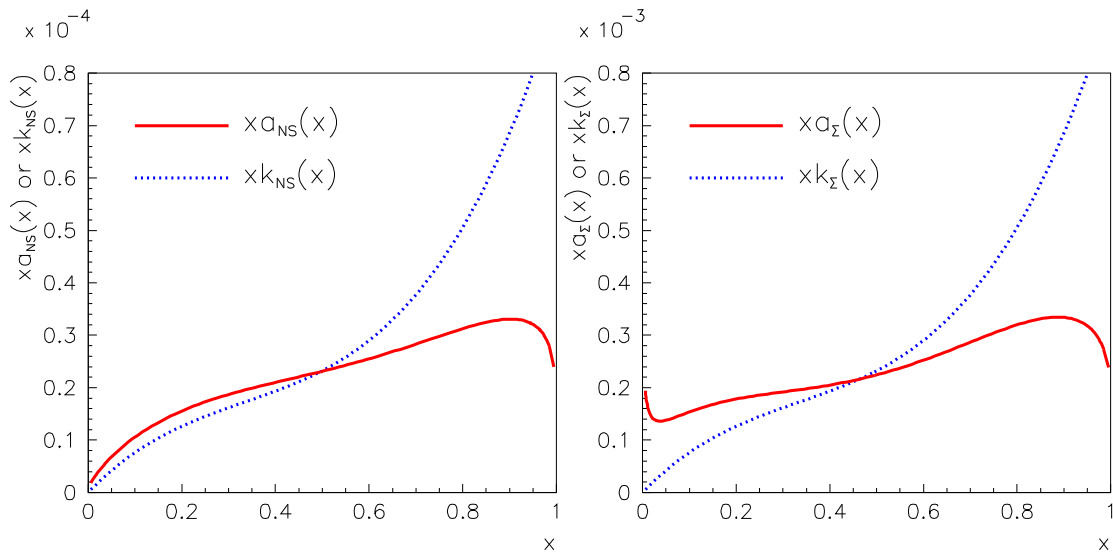
$$q_T^{\text{QED}} \rightarrow (x^2 + (1 - x)^2) \ln \frac{Q^2}{xP^2} + 8x(1 - x) - 2, \quad x(1 - x)P^2 \gg m_q^2$$

$$q_L^{\text{QED}} = \frac{4x^2(1 - x)^2 P^2}{x(1 - x)P^2 + m_q^2} \rightarrow 4x(1 - x); \quad x(1 - x)P^2 \gg m_q^2$$

$$\rightarrow \frac{P^2}{m_q^2} 4x^2(1 - x)^2; \quad x(1 - x)P^2 \ll m_q^2$$

QCD corrections **soften quarks** and **generate** gluons.

at large  $Q^2$  :  $q_T^{\text{QCD}}(x, Q^2) \rightarrow a(x) \ln Q^2$



Points on  $\gamma_T^*$  to keep in mind:

- $\ln Q^2$  rise is a purely **QED effect!**
- **QCD** effect: the difference  $[a(x) - (x^2 + (1 - x)^2)]$
- $f^{\text{HAD}}$  drop with  $P^2$  **much faster** than  $f^{\text{PL}}$  and for  $P^2 \gtrsim 2 \text{ GeV}^2$  become practically **negligible**.

## The concept of $\gamma^*$ structure in QCD

In QCD the extent to which the effects of  $\gamma^*$  are included depends on particular theoretical framework adopted. Questions we have often encountered:

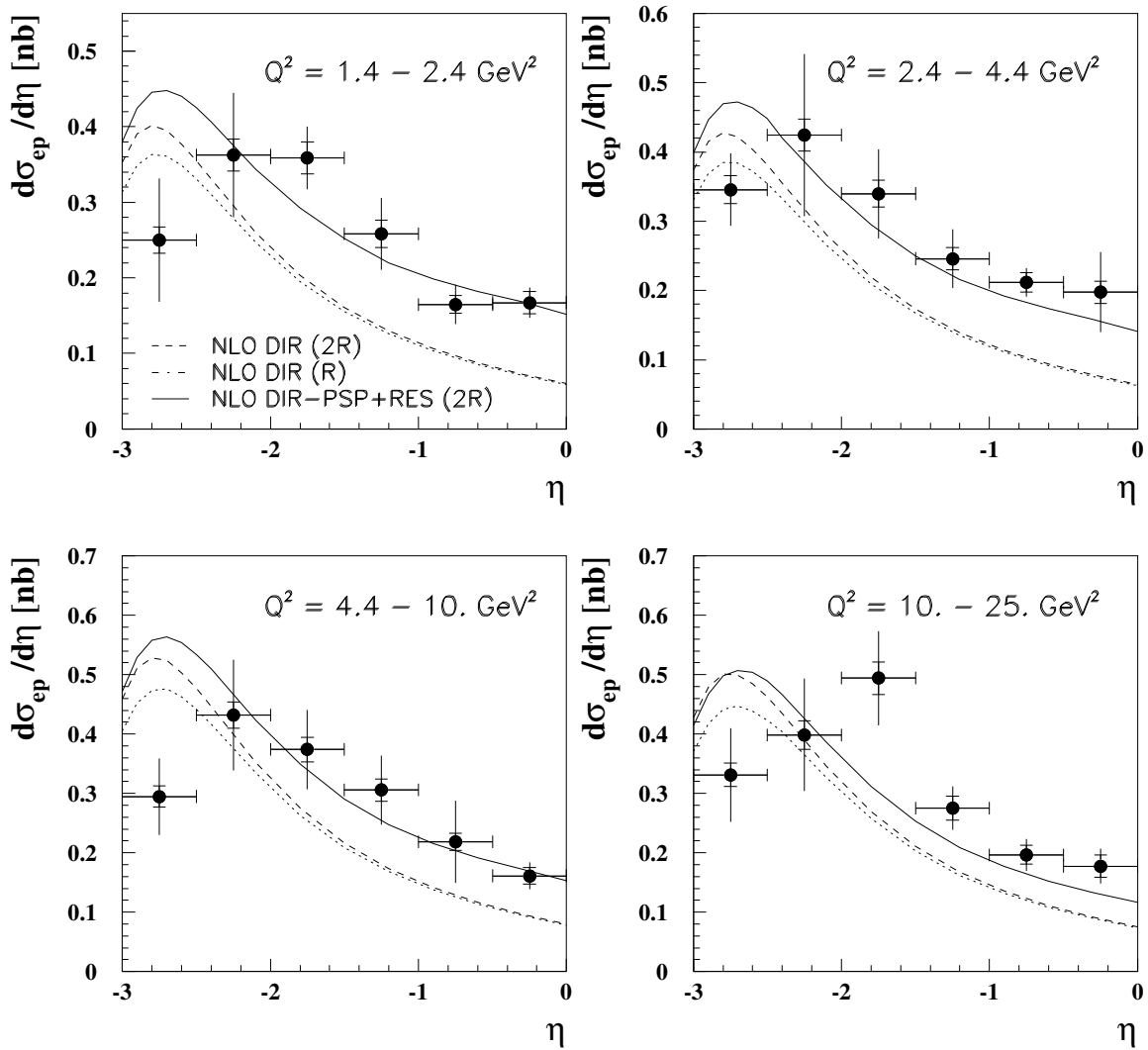
- a) **Why** to introduce the concept of  $\gamma^*$  **structure** when we have exact NLO QCD programs like **DISENT, MEPJET, DISASTER**, which dispense with this concept?
- b) Is there **any evidence** for the usefulness of this concept in available data?
  - ad a) There is a **large difference** in part of the phase space accessible at HERA between the results of NLO calculations **with and without** the resolved  $\gamma^*$  contributions.
  - ad b) **YES!** NLO calculations without the resolved  $\gamma^*$  contribution are **significantly below** the data in the region of moderate  $P^2 \ll Q^2 \simeq E_T^2$  and  $\eta^* \simeq 0$

Summary: *in principle* the concept of  $\gamma^*$  structure **need not be introduced** but *in practice* it is **extremely useful** as a way of approximately including part of **higher order** perturbative QCD corrections

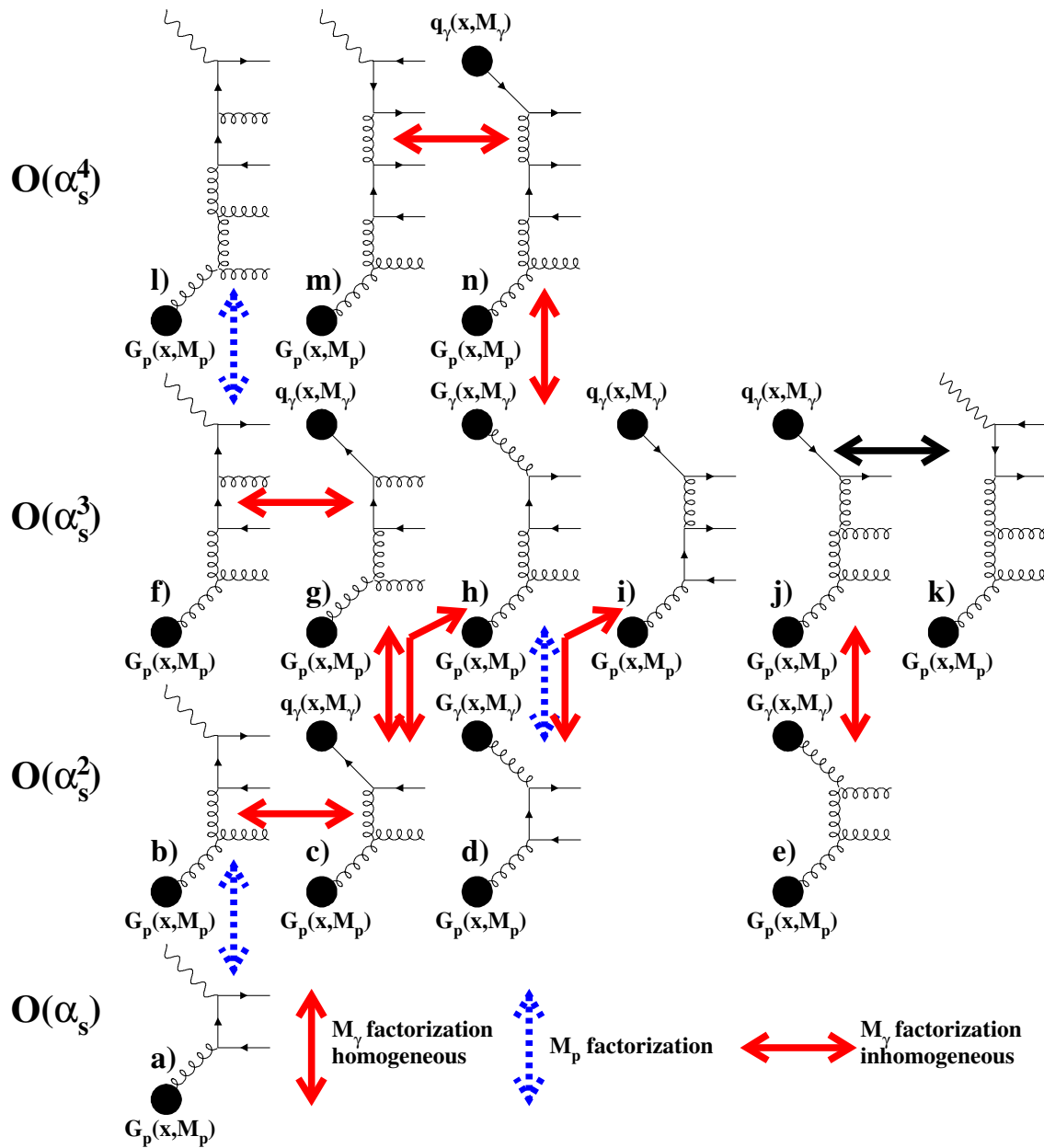
Example: [J. Cvach](#): Talk at DIS99:

## H1 Preliminary

ASYM.  $E_T$  (5/7 GeV)



Factorization scale dependence and the relation between direct and resolved photon contributions:





## Resolved $\gamma_{T,L}^*$ in QCD calculations

- **LO MC event generators:**

Contributions of  $\gamma_L^*$  included exactly in the **direct** channel. In the resolved one

**PYTHIA:** since version 6.12  $f_{\gamma_T^*/e}$  as well as  $f_{\gamma_L^*/e}$  with exact kinematics at the  $e\gamma^*e$  vertex and SaS PDF of  $\gamma_T^*$ .  $\gamma_L^*$  treated via **rescaling ansatz**.

**HERWIG:**

official version:  $\gamma_T^*$  only

my version:  $\gamma_L^*$  as well with QCD improved PDF

**PHOJET:** only  $\gamma_T^*$

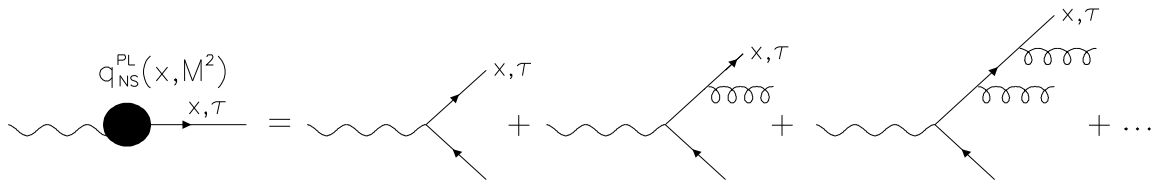
- **NLO parton level calculations:**

**DISENT, MEPJET, DISASTER:**  $\gamma_{T,L}^*$  treated exactly up to order  $\alpha\alpha_s^2$ , but only **unsubtracted direct** contributions taken into account

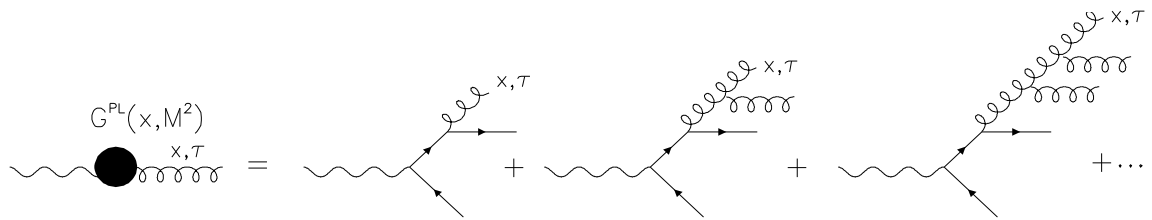
**JETVIP:** includes the **resolved photon** channel with  $\gamma_T^*$  convoluted with cross sections up to  $\alpha_s^3$  recently we have added (with help from Bjorn Pötter) the **resolved  $\gamma_L^*$**  contributions (see below)

# QCD improved PDF of $\gamma_L^*$

Resummation of diagrams



in **leading-log approximation** (i.e. in powers of  $\alpha_s \ln M^2$ ) and similarly for quark singlet and gluons



leads for

$$m_q^2 \ll P^2 \ll M^2$$

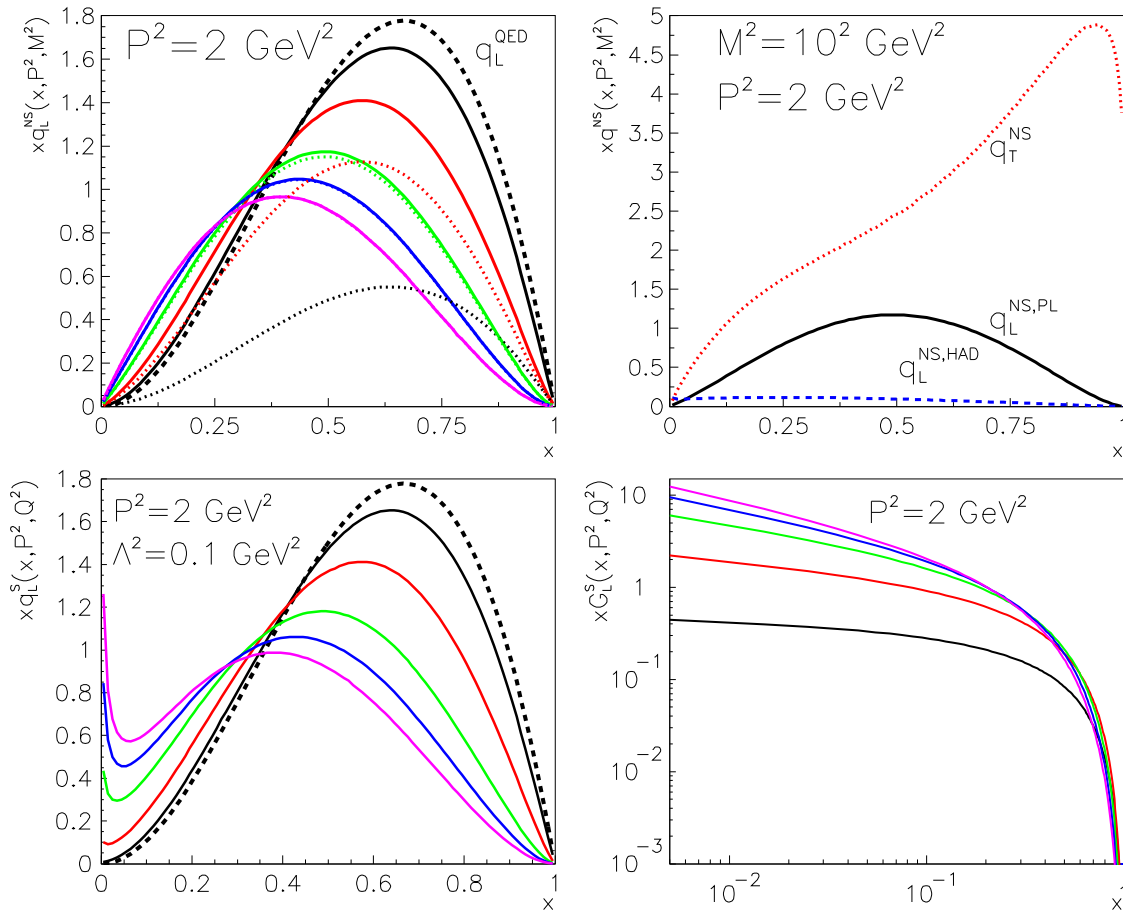
to typical **hadron-like scale dependence** even for the **pointlike parts!**

$$q_L^{NS}(n, P^2, M^2) = k_L(n) \left[ \frac{\alpha_s(M^2)}{\alpha_s(P^2)} \right]^{-2P_{qq}^{(0)}(n)/\beta_0},$$

where

$$k_l(x) = 12x(1-x), \quad s \equiv \frac{\ln(M^2/\Lambda^2)}{\ln(P^2/\Lambda^2)}$$

Examples:



**Hadronic** part of  $q_L^{\text{QCD}}$  negligible for  $P^2 \gtrsim 2 \text{ GeV}^2$

Parameterization of PDF of  $\gamma_L^*$  available for

$$0.001 \leq x \leq 0.995, \quad 1 \leq s \leq 3.9$$

**Question:** what is  $m_q$  or, generally, what governs the onset of PDF of  $\gamma_L^*$ ?

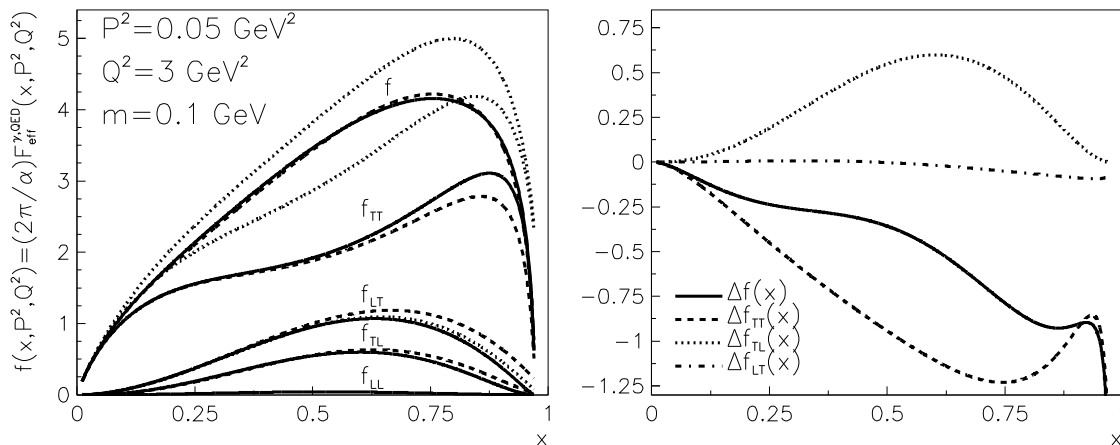
**The relevance of  $\gamma_L^*$**

**Claim:** whenever the variations of contributions of  $\gamma_T^*(P^2)$  with  $P^2$  are taken into account, so **must** be those of  $\gamma_L^*(P^2)$ !

Illustration: at LEP one measures the combination

$$F_{\text{eff}}^\gamma(x, P^2, Q^2) \equiv \frac{Q^2}{4\pi^2\alpha} (\sigma_{TT} + \sigma_{LT} + \sigma_{TL} + \sigma_{LL})$$

The QED structure function  $F_{\text{eff}}^{\text{QED}}$ , measurable using  $\mu^+\mu^-$  pairs, is fully calculable. For **OPAL** data the individual contributions  $\sigma_{ij}$  look as follows



The data clearly require the contributions of target  $\gamma_L^*$ .  
The same for **L3** data.

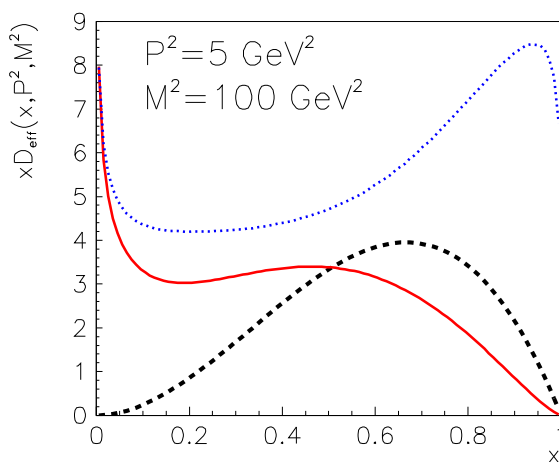
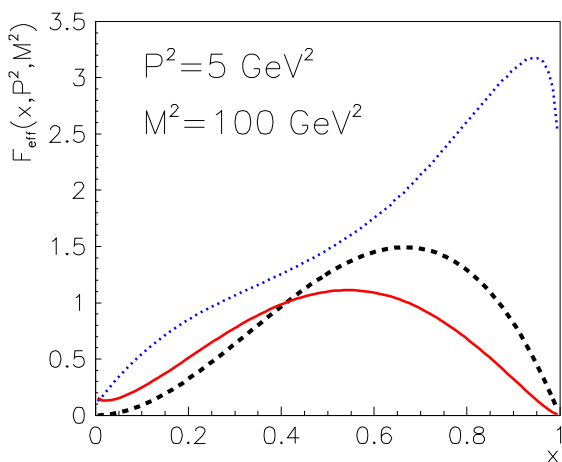
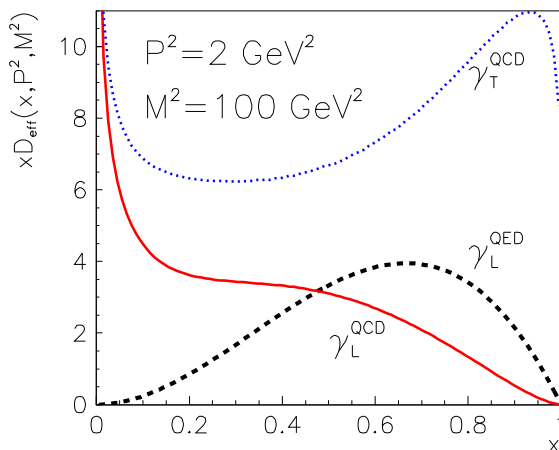
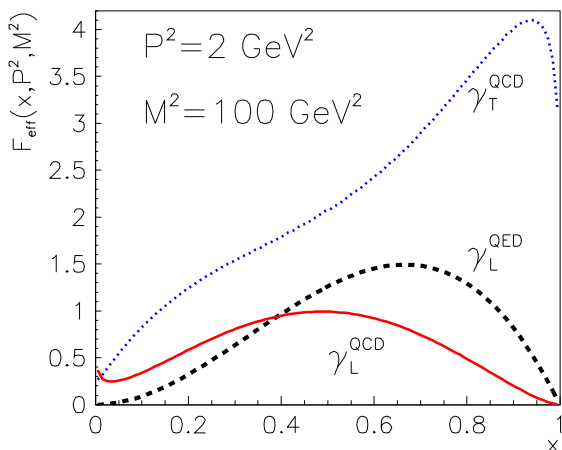
## Resolved $\gamma_L^*$ in LO calculations

The relative contributions of  $\gamma_L^*$  depend on

- electron variables  $y$  and  $P^2$
- jet variables  $E_T$ ,  $\eta$  and  $x_\gamma$ .

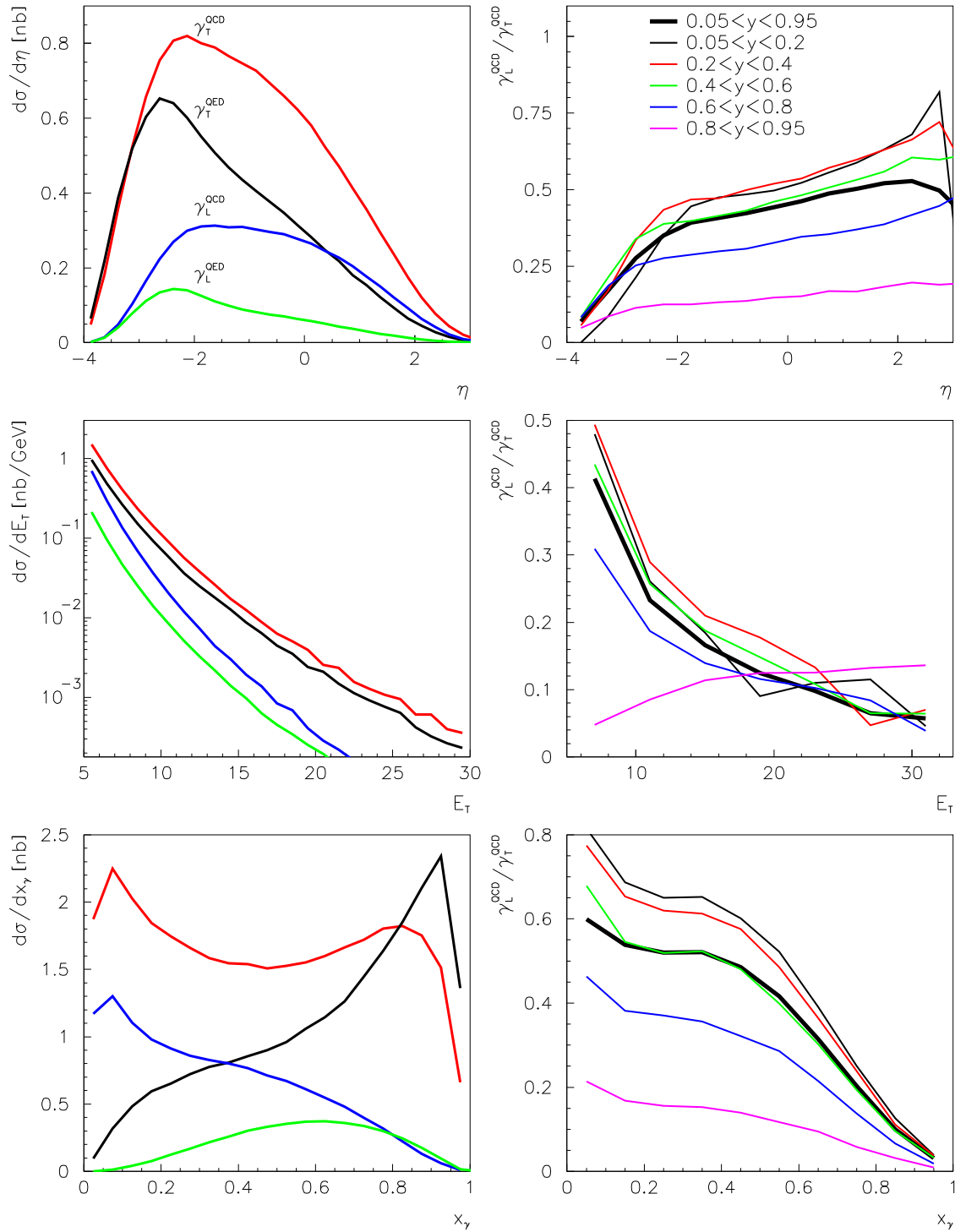
Analytical evaluation of  $F_{\text{eff}}(P^2, M^2)$  and

$$D_{\text{eff}}(x, P^2, M^2) \equiv \sum_{i=1}^{n_f} (q_i + \bar{q}_i) + \frac{9}{4}G$$

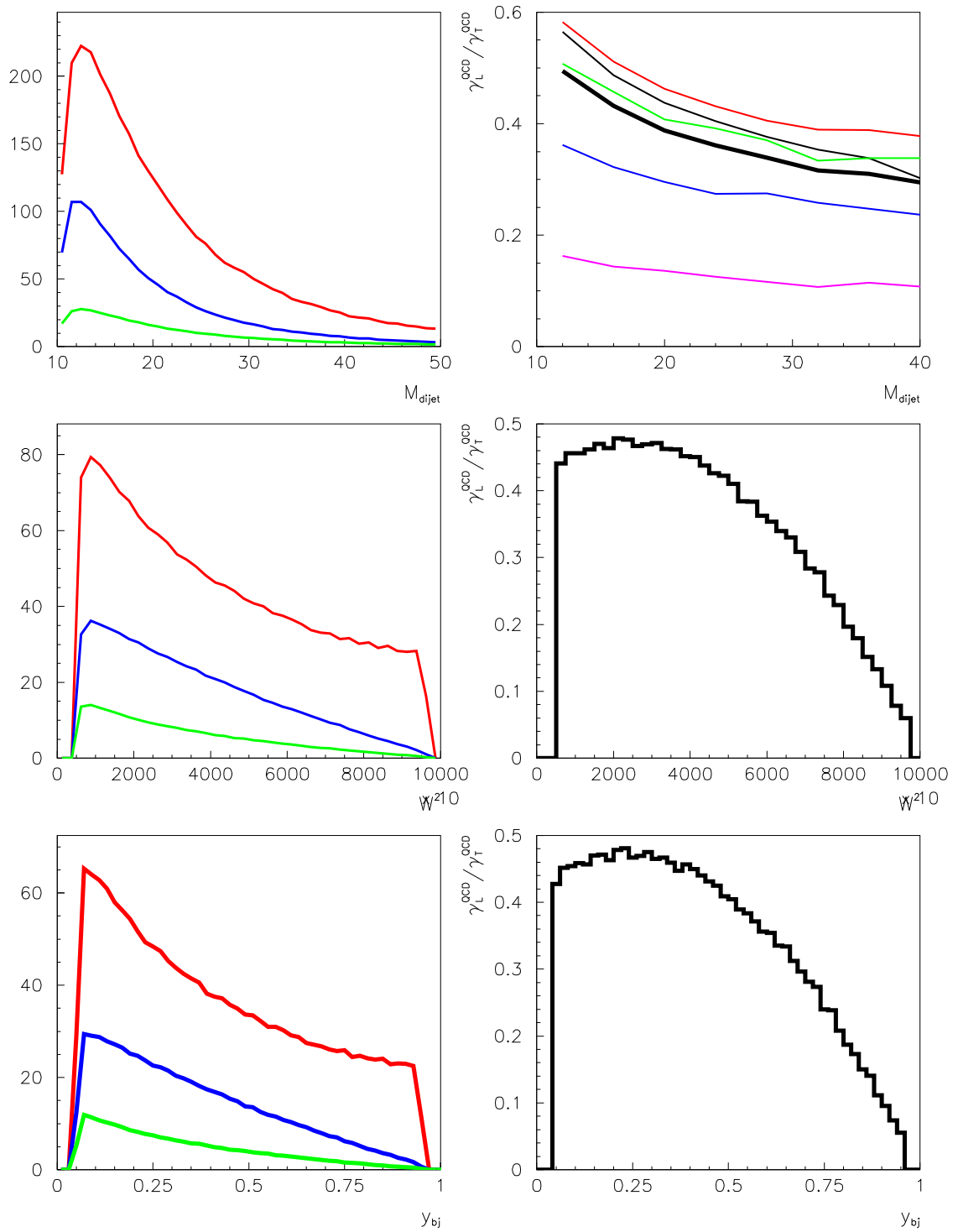


# HERWIG MC simulations:

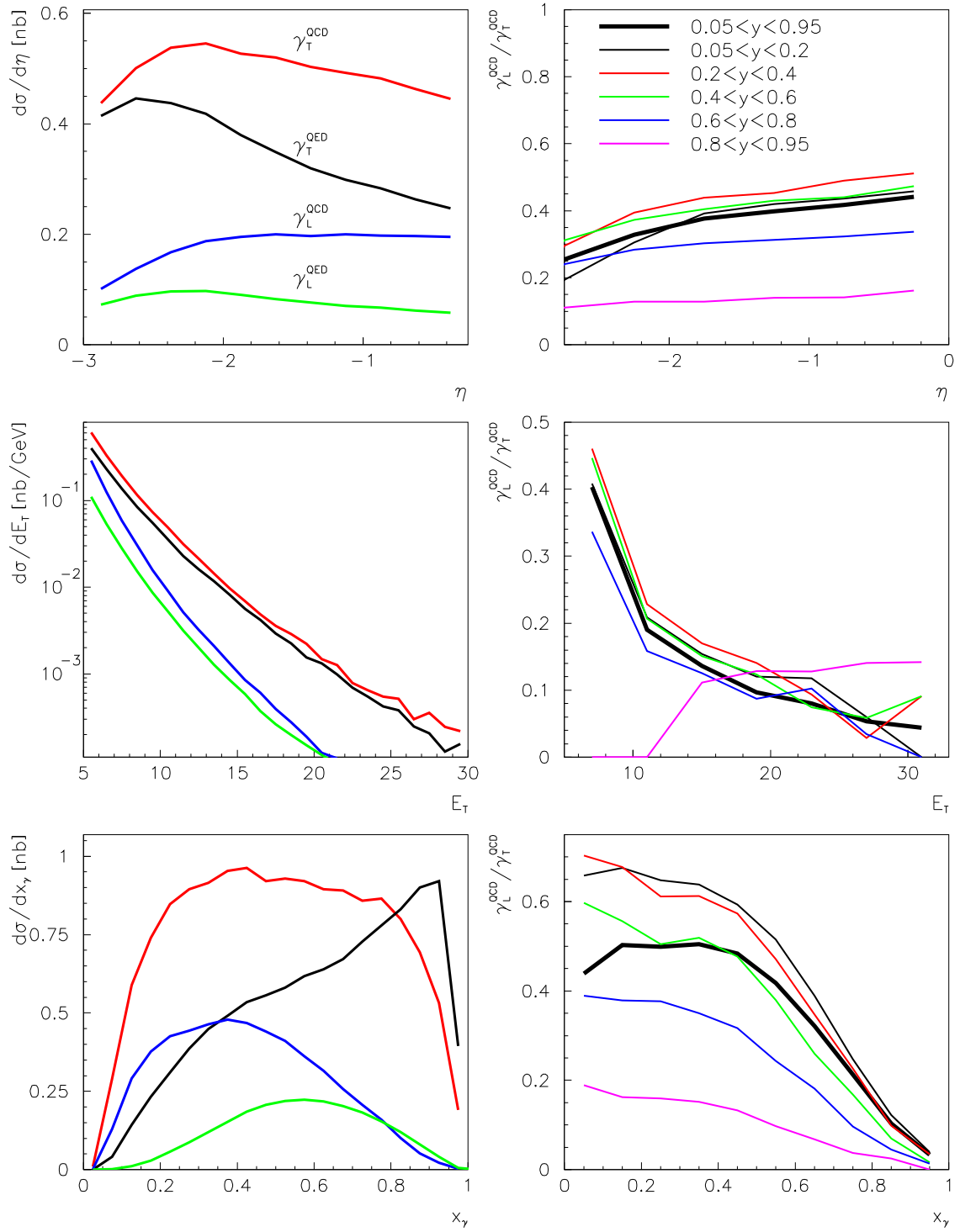
$1.4 < P^2 < 2.4 \text{ GeV}^2, 0.05 < y < 0.95, E_T > 5 \text{ GeV}, -5 < \eta < 5$



$1.4 < P^2 < 2.4 \text{ GeV}^2, 0.05 < y < 0.95, E_T > 5 \text{ GeV}, -5 < \eta < 5$

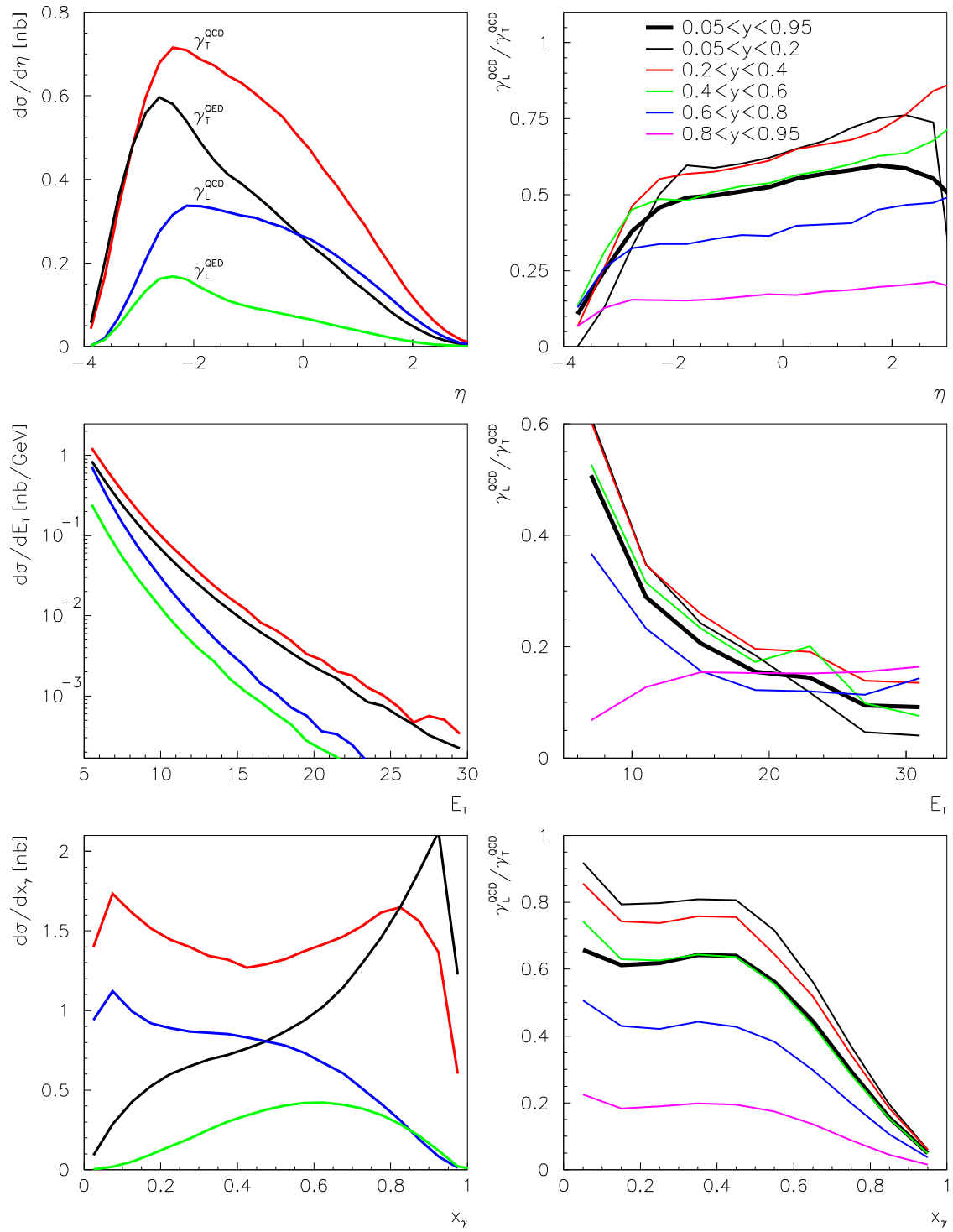


$1.4 < P^2 < 2.4 \text{ GeV}^2, 0.05 < y < 0.95, E_T > 5 \text{ GeV}, -3 < \eta < 0$

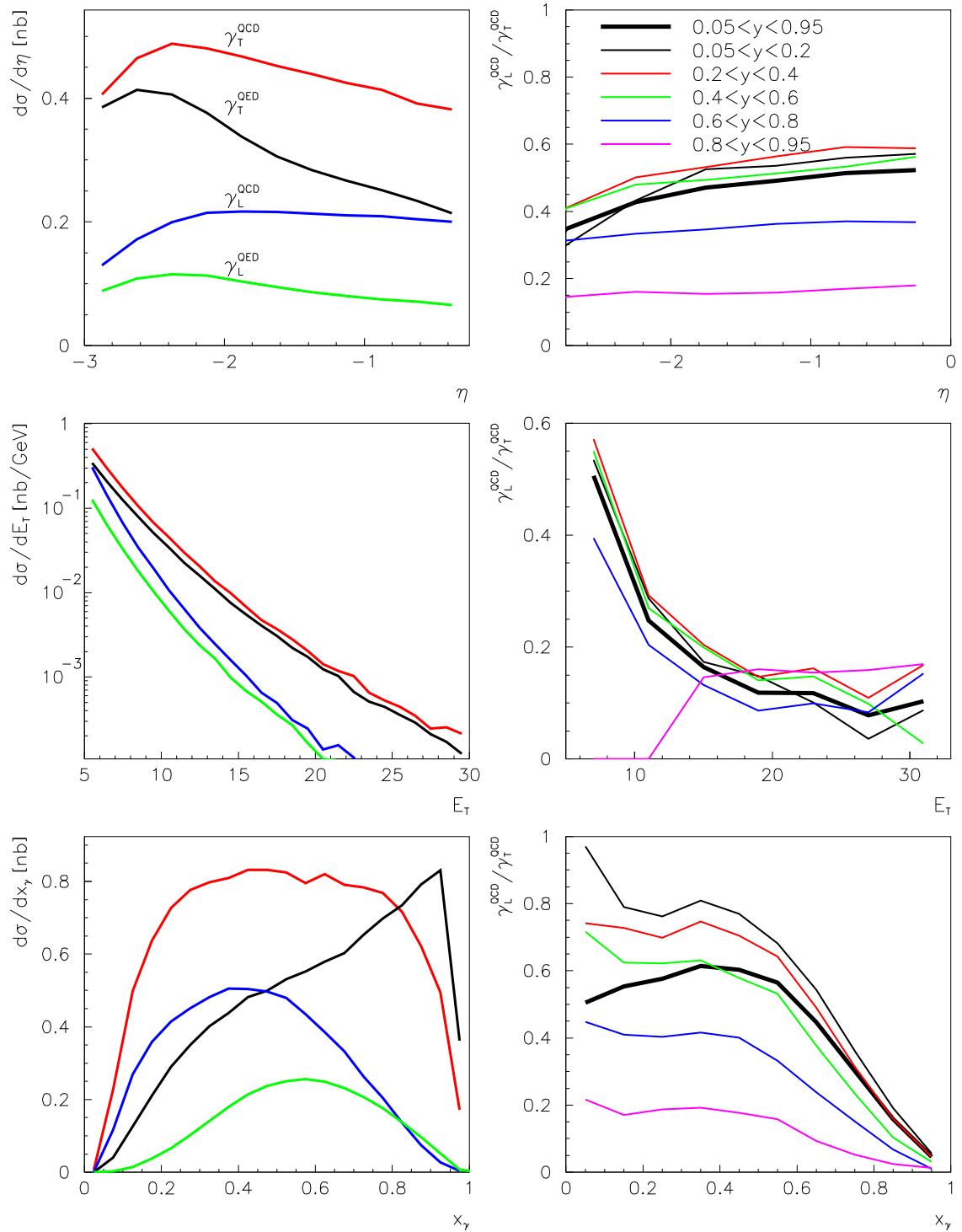




$2.4 < P^2 < 4.4 \text{ GeV}^2, 0.05 < y < 0.95, E_T > 5 \text{ GeV}, -5 < \eta < 5$



$2.4 < P^2 < 4.4 \text{ GeV}^2, 0.05 < y < 0.95, E_T > 5 \text{ GeV}, -3 < \eta < 0$



## Message from the comparisons

In the kinematical region

$$\Lambda^2 \ll P^2 \ll Q^2$$

accessible at HERA and conventionally considered as part of **DIS** region the contributions of  $\gamma_L^*$  are **substantial**, particularly

- at **small**  $y$ ,
- close to  **$E_T$  threshold**,
- for **small**  $x_\gamma$ ,
- i.e. **large**  $\eta$

The cuts enforced by H1 and ZEUS acceptances reduce the sensitivity to contributions of  $\gamma_L^*$ , but in parts of accessible kinematical range they are typically  $\gtrsim 50\%$  and can be identified by their

**characteristic  $y$  and  $P^2$  dependence.**

## Resolved $\gamma_L^*$ in JETVIP calculations of dijet production at HERA

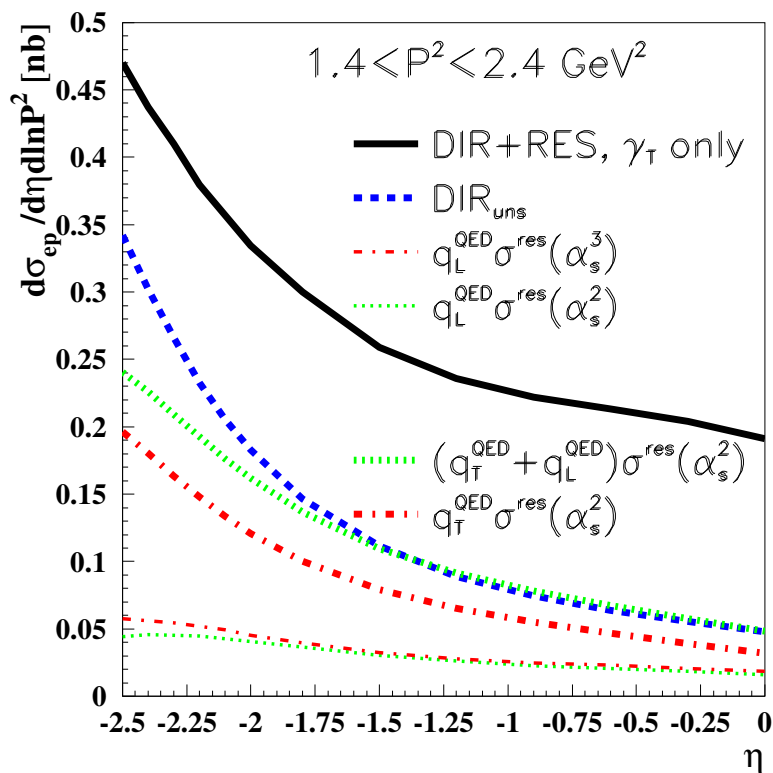
Standard formulation:  $\gamma_L^*$  included **exactly in direct unsubtracted calculations** (LO as well as NLO) but **not in the resolved photon** contributions.

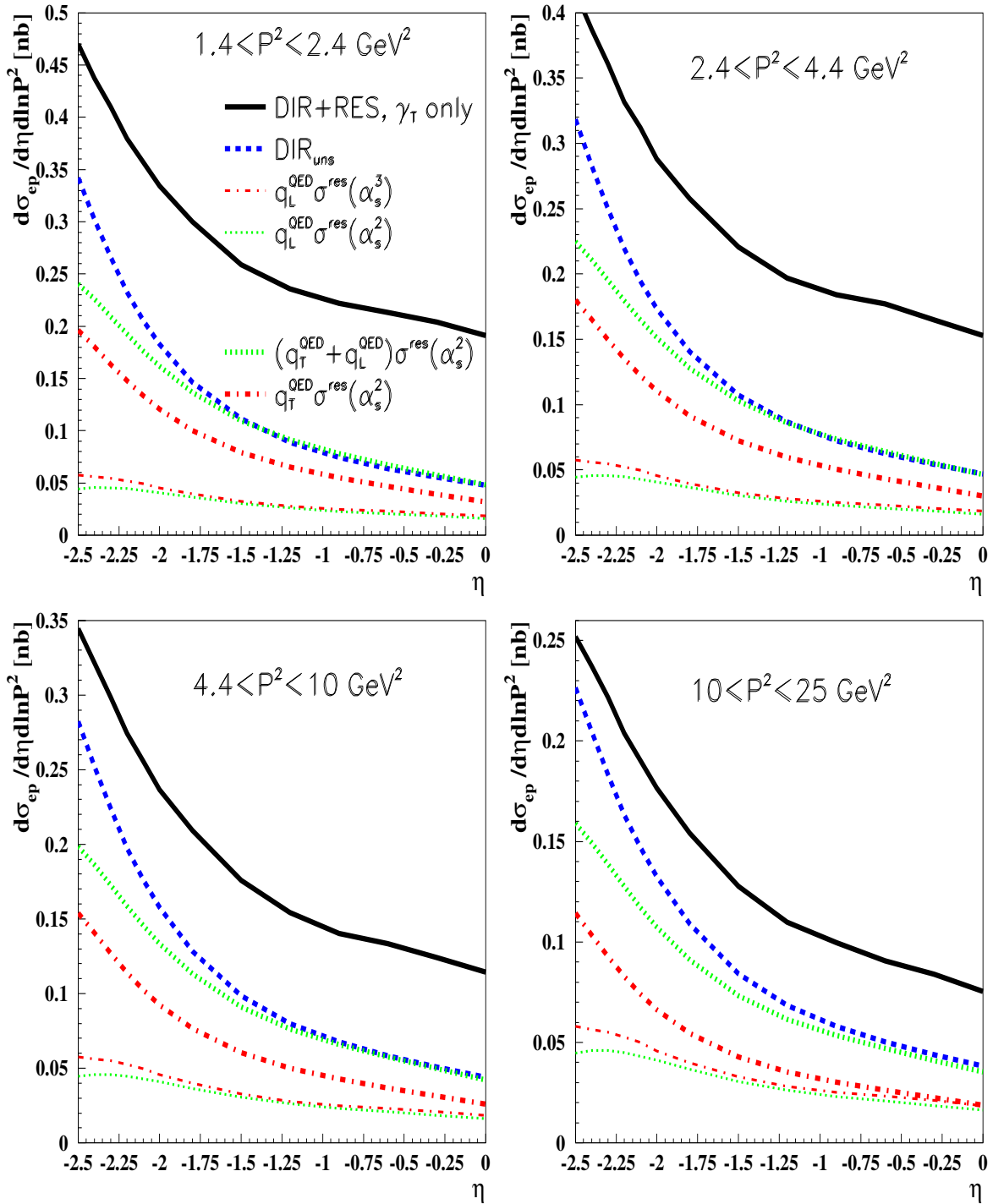
Schematically:

$$\begin{aligned} \sigma(\text{TOT}) = & \sigma(\text{DIR}_{\text{uns}}) - \sigma_T(\text{PSP}) + \sigma_T(\text{RES}) \\ & - \sigma_L(\text{PSP}) + \sigma_L(\text{RES}) \end{aligned}$$

Calculations performed for **asymmetric  $E_T$  cuts**:

$$E_T^{(1)} \geq 7, \quad E_T^{(2)} \geq 5 \text{ GeV}$$



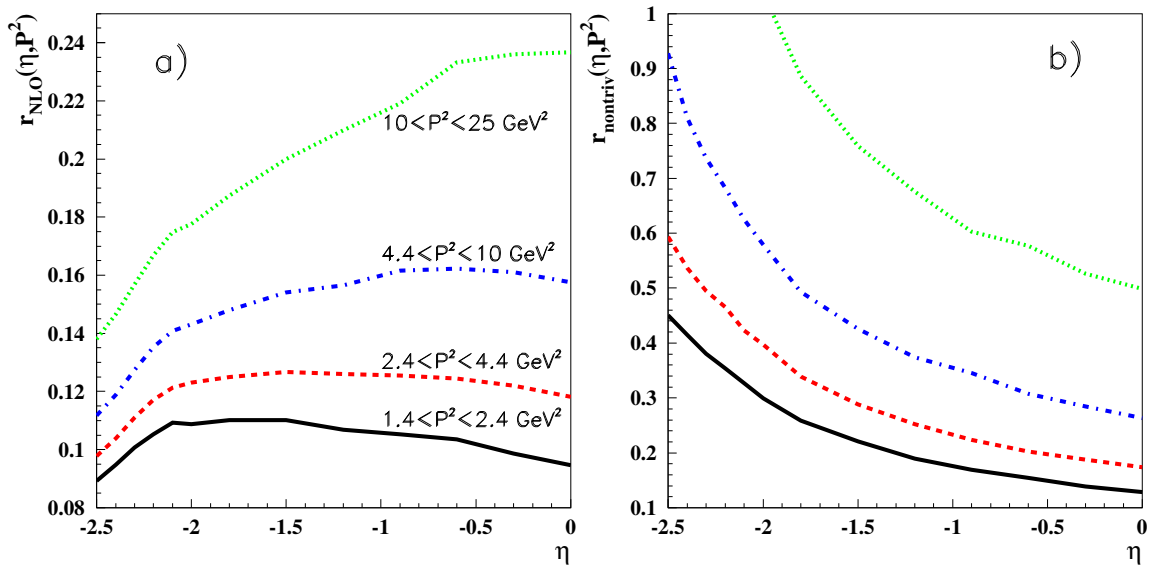


Nontrivial effect of introducing the concept of PDF of  $\gamma_L^*$  into JETVIP measured by the ratio

$$r_q^{\text{NLO}} \equiv \frac{(q_L^{\text{QCD}} - q_L^{\text{QED}}) \otimes \sigma_q^{\text{res}}(\alpha_s^2) + q_L^{\text{QCD}} \otimes \sigma_q^{\text{res}}(\alpha_s^3)}{\sigma^{\text{DIR+RES}}(\gamma_T)}$$

$$r_G^{\text{NLO}} \equiv \frac{G_L^{\text{QCD}} \otimes (\sigma_G^{\text{res}}(\alpha_s^2) + \sigma_G^{\text{res}}(\alpha_s^3))}{\sigma^{\text{DIR+RES}}(\gamma_T)}.$$

Effects of  $q_L^{\text{QED}}$ :



We wanted to present first NLO JETVIP results with  $q_L^{\text{QCD}}$  and  $G_L^{\text{QCD}}$  but failed because of other duties. Hope to have them for the Proceedings.

## Future

**Experiment:** ongoing analysis of **H1** dijet data (31 pb<sup>-1</sup>,  $1.4 \leq P^2 \leq 50 \text{ GeV}^2$ ,  $0.1 \leq y \leq 0.9$ )

$E_T^{\min}$	$N_{tot}$	1.4–2.4	2.4–4.4	4.4–10	10–25
5 GeV	123000	18400	25500	31800	30700
6 GeV	80000	12300	16500	20400	20000
7 GeV	53000	7600	11200	13000	13000
10 GeV	17500	2400	3200	4300	4300

offers a chance to

- perform the comparison with QCD calculations in the kinematical region  $P^2 \ll Q^2$  in greater detail
- identify the contributions of  $\gamma_L^*$  by measuring  $D_{\text{eff}}^{\gamma_L}(x, P^2, Q^2)$

For the second task one has to separate  $\gamma_L^*$  by measuring the dependence of dijet cross sections on

- $y$ :  $\sigma_L \propto (1 - y) \Rightarrow$  broad range in  $y$  necessary
- $P^2$ :  $\sigma_L \propto P^2 \Rightarrow$  **VLQ** ( $P^2 \simeq 0.1 - 0.2$ ) vital!
- $E_T$ : **hadronic** scaling violations of  $q_L(x, P^2, M^2)$

**Theory:** detailed studies using **JETVIP** with QCD improved PDF of  $\gamma_L^*$

## Conclusions

1. The concept of **resolved**  $\gamma_L^*$  is phenomenologically **very useful**.
2. Contributions of resolved  $\gamma_L^*$  **must be included** whenever virtuality dependence of PDF  $\gamma_T^*$  is taken into account.
3. Numerically these contributions are **quite large** in parts of phase space accessible at HERA.
4. QCD improved PDF of  $\gamma_L^*$  are **available** but more theoretical work needed, in particular concerning the question of their threshold behavior.
5. There is a good chance to **extract** PDF of  $\gamma_L^*$  from recent HERA data.